

Molecular Simulation

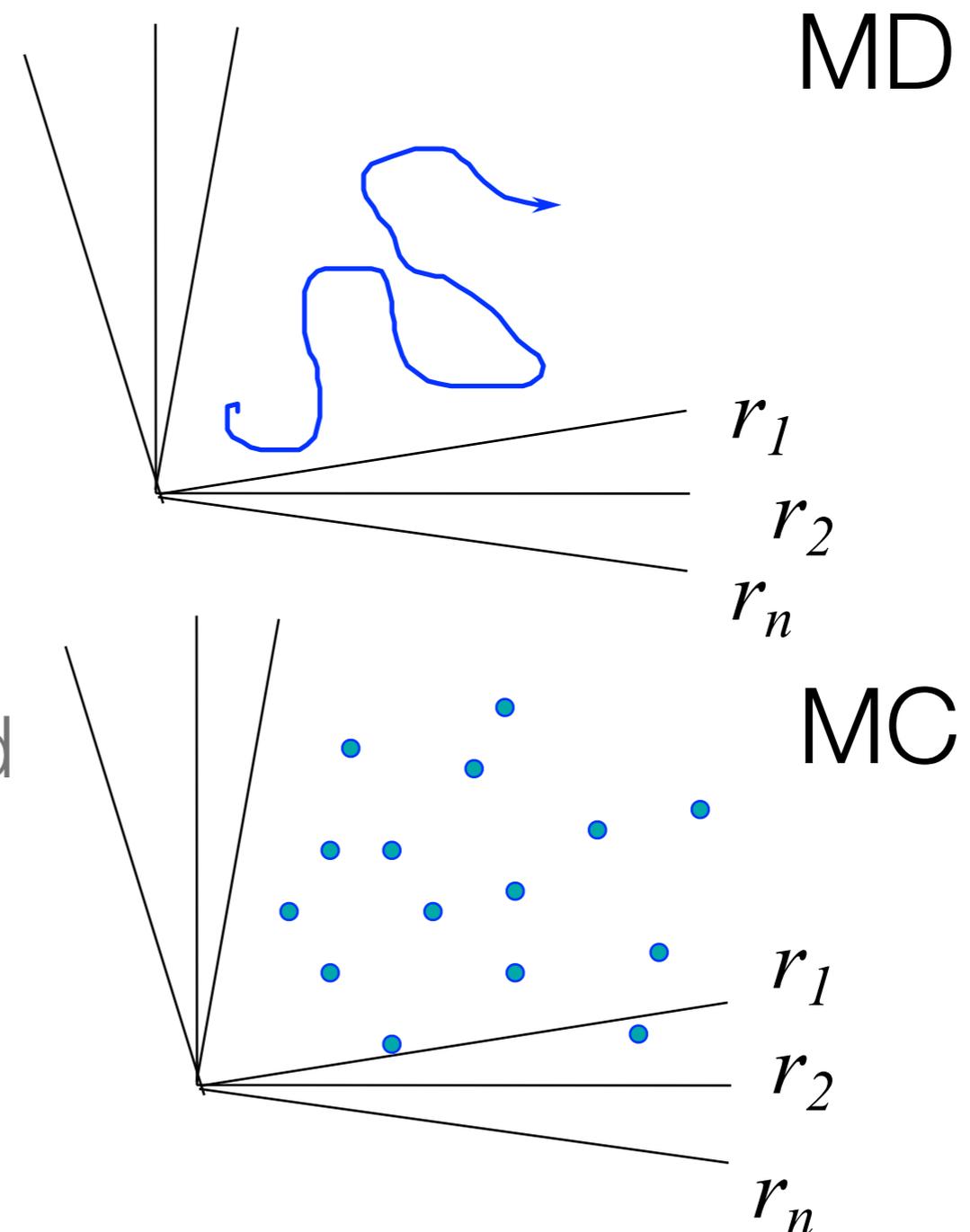
Introduction

Introduction

- Why to use a simulation
- Some examples of questions we can address

Molecular Simulations

- **Molecular dynamics:** solve equations of motion
- **Monte Carlo:** importance sampling
- Calculate thermodynamic and transport properties for a given intermolecular potential



Uses of Molecular Simulations

We assume the interactions between the particles are known!

Exact= in the limit of infinitely long simulations the error bars can be made infinitely small

The idea for a given *intermolecular potential* “*exactly*” compute the *thermodynamic* and *transport* properties of the *system*

If one could envision an experimental system of these N particles that interact with the potential.

Pressure
Heat capacity
Heat of adsorption
Structure
....

Diffusion coefficient
Viscosity
...

Why Molecular Simulations

Paul Dirac, after completing his formalism of quantum mechanics: “*The rest is chemistry...*”.

This is a heavy burden the shoulders of “chemistry”:

The “*rest*”:

amounts to the *quantitative description* of the world around us and the prediction of all every-day phenomena ranging from the chemical reactions of small molecules to the integrated description of living organisms.

Intermolecular potential

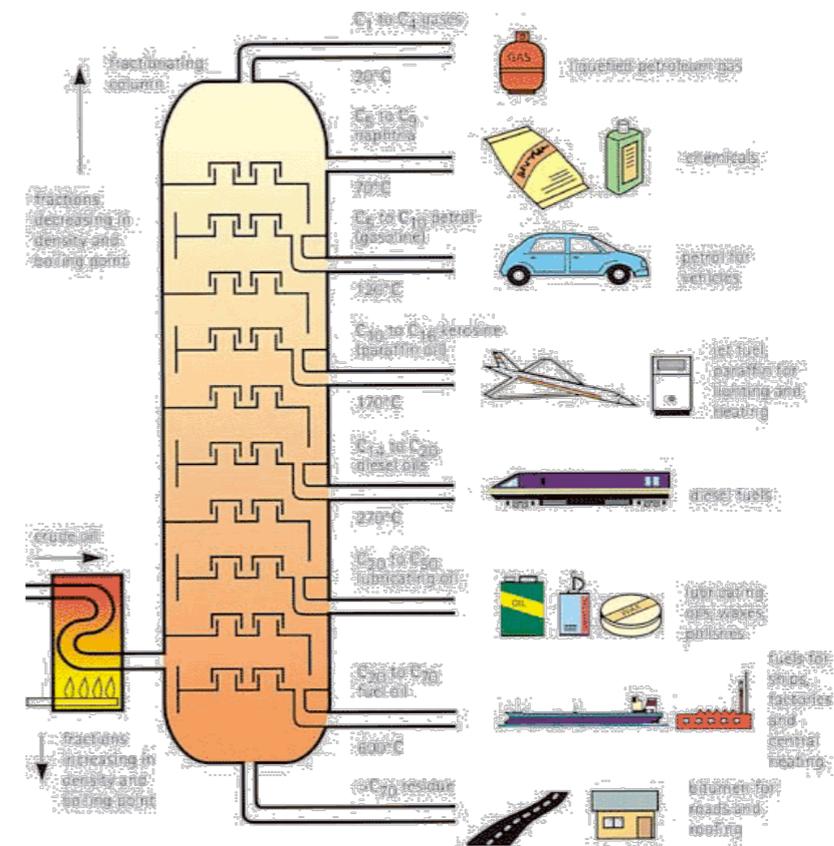
The intermolecular potential can:

- Mimic the experimental system as accurate as possible:
 - Replace experiments (dangerous, impossible to measure, expensive, ...)
- Make a model system:
 - Test theories that can not directly be tested with experiment

If we know/guess the “true” intermolecular potential

Example 1: Mimic the “real world”

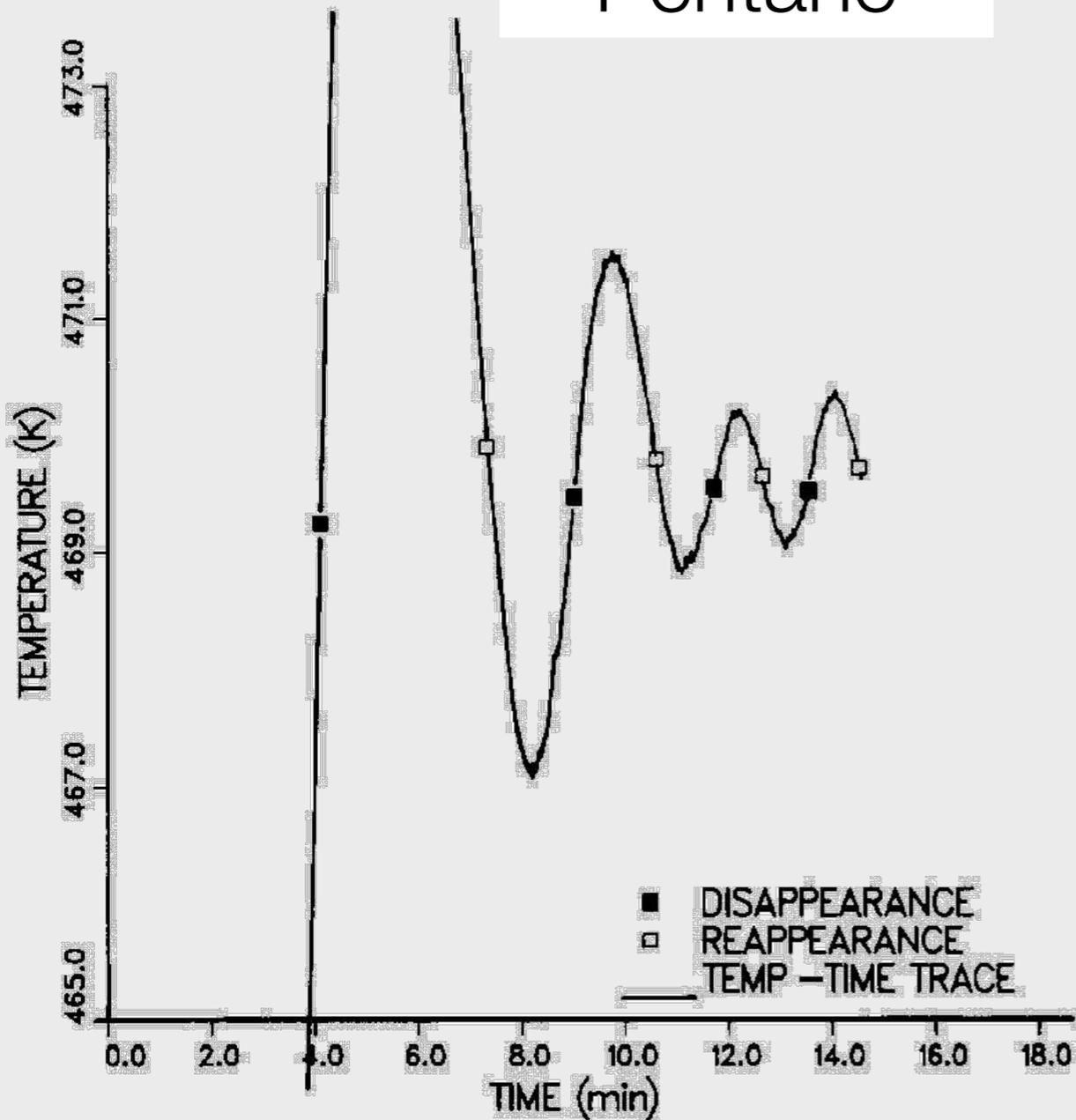
Critical properties of long chain hydrocarbons



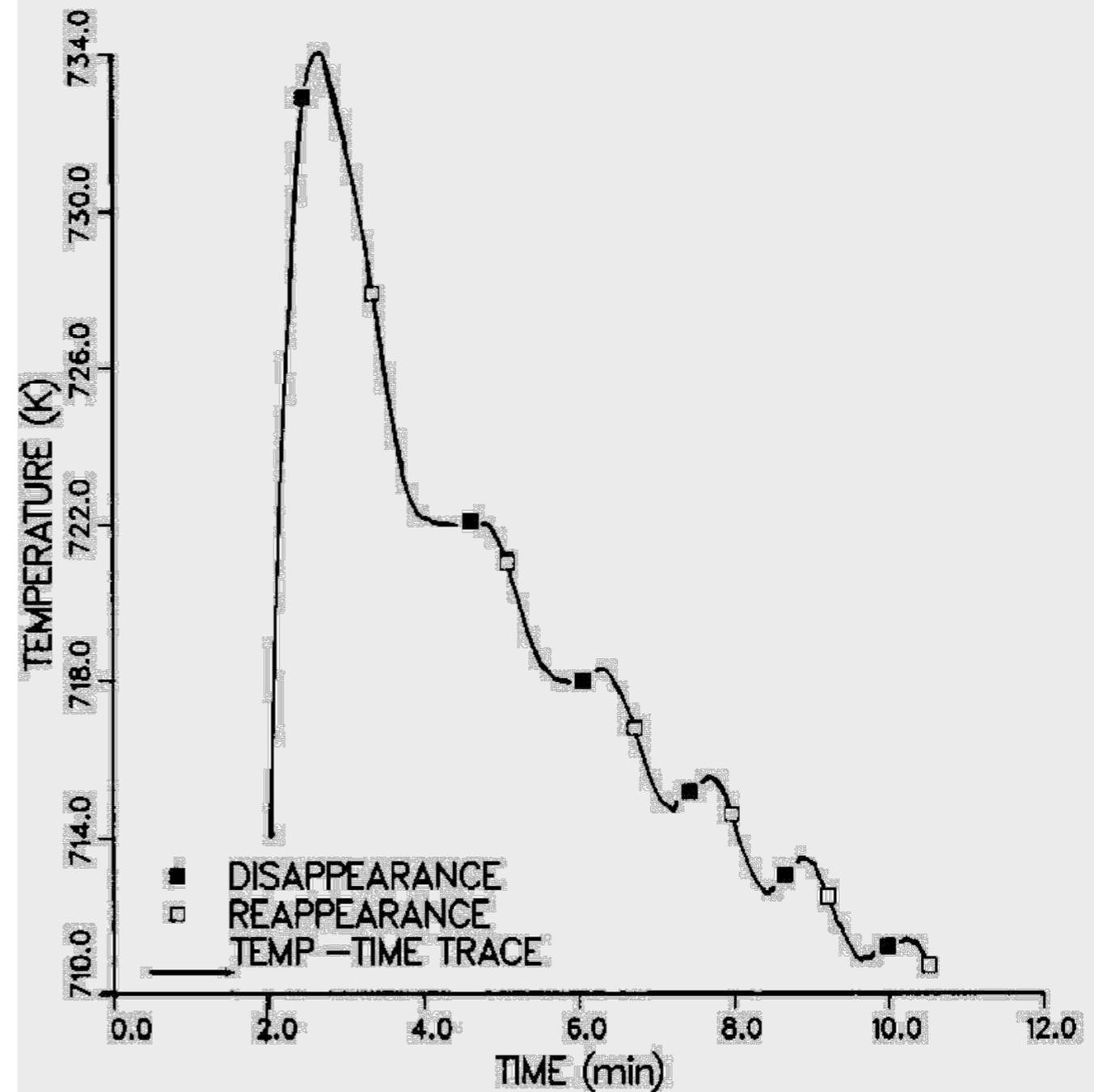
To *predict* the thermodynamic properties (boiling points) of the hydrocarbon mixtures it is convenient (=Engineering models use them) to know the critical points of the hydrocarbons.

Critical points of long chain hydrocarbons

Pentane



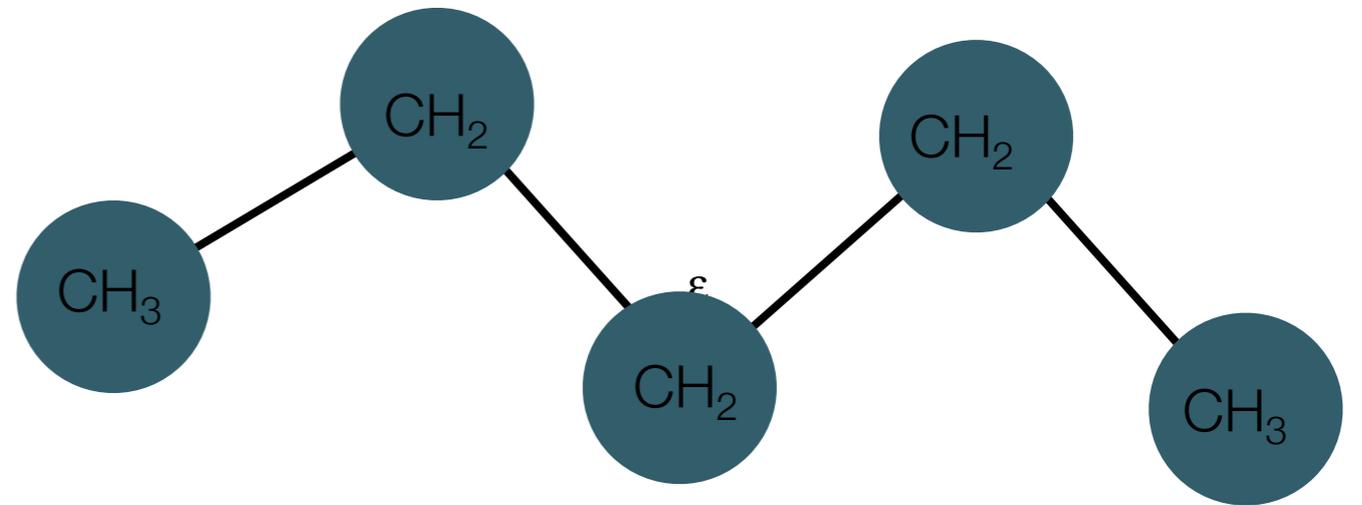
Heptadecane



Hydrocarbons: intermolecular potential

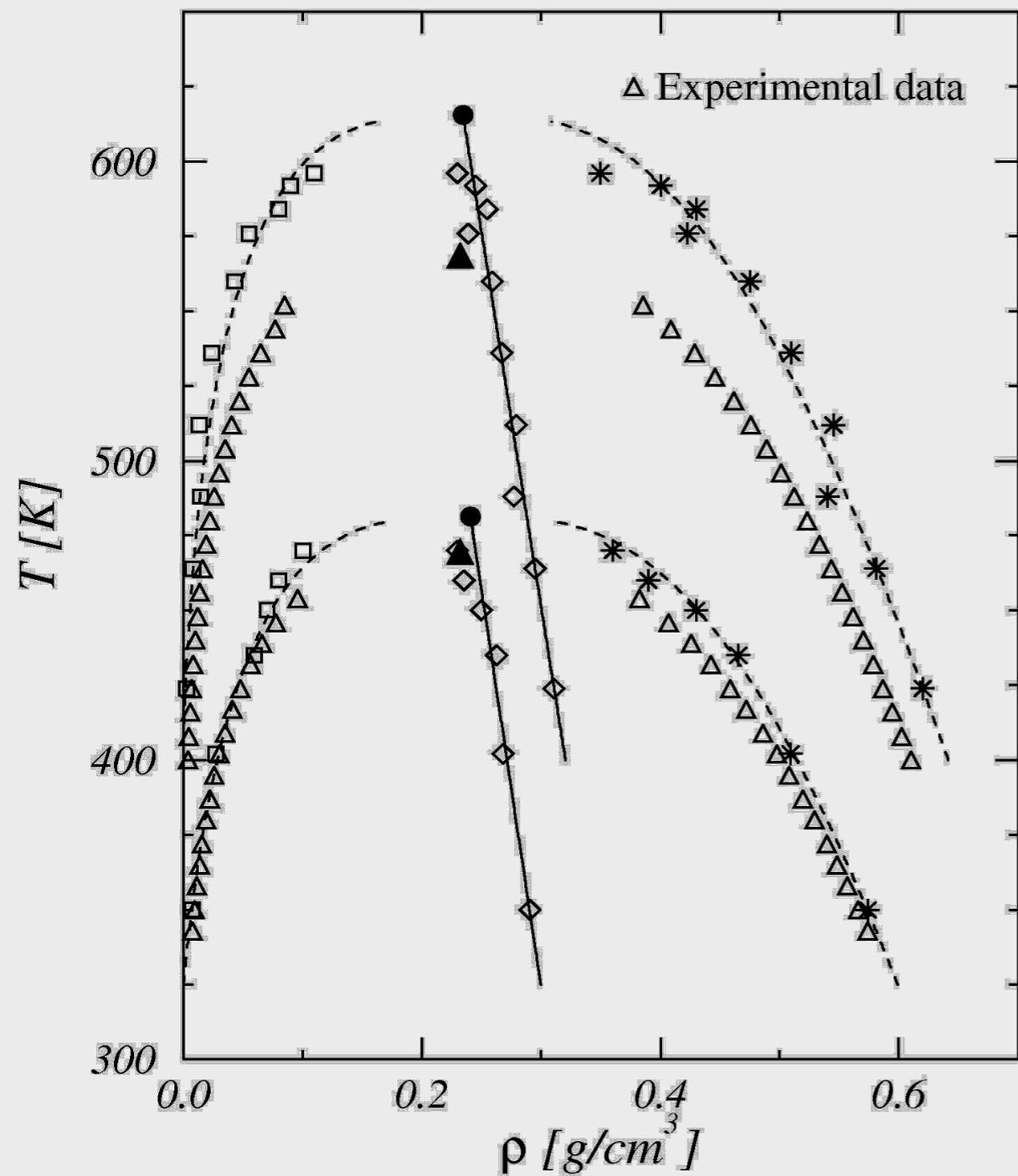
United-atom model

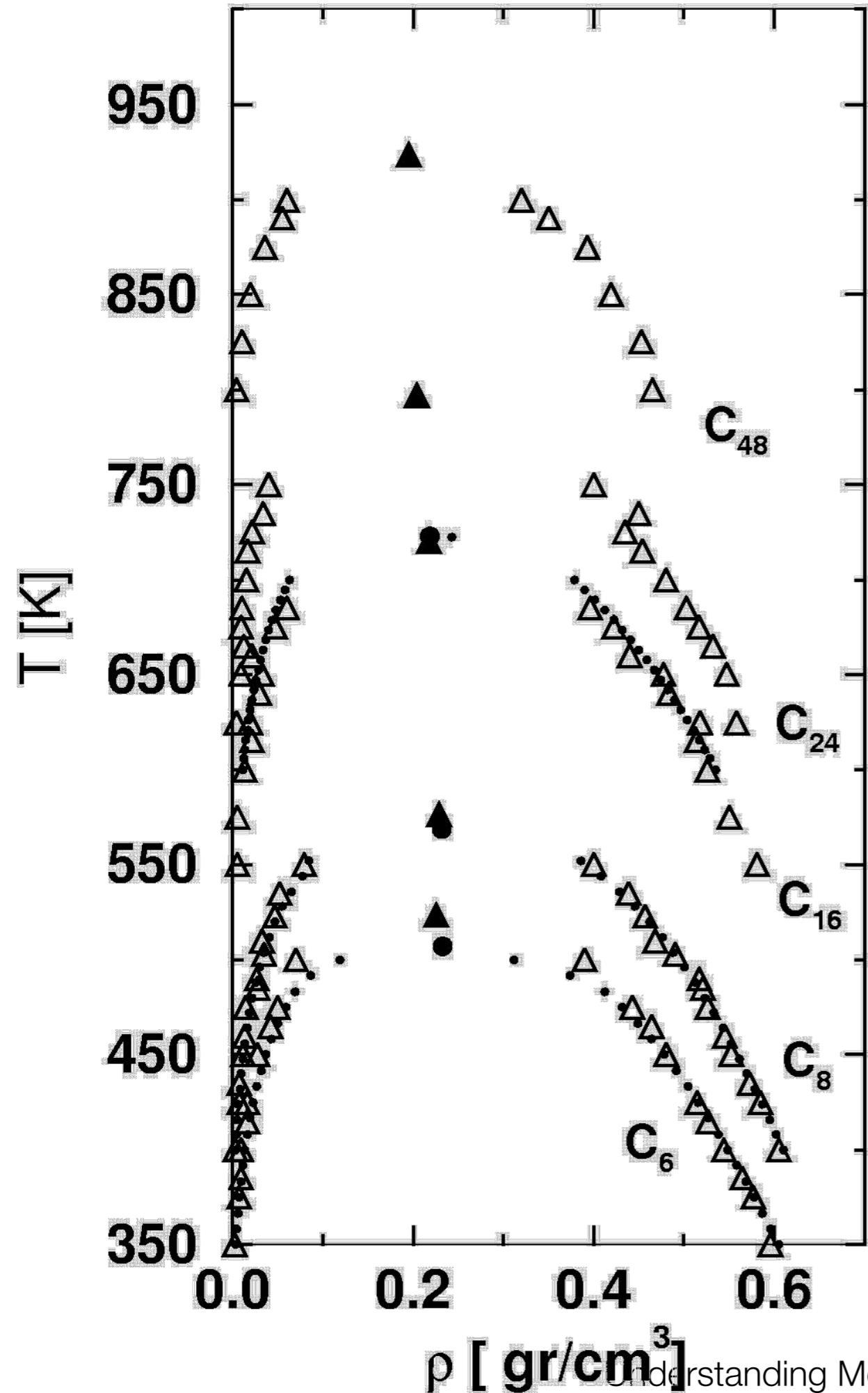
- Fixed bond length
- Bond-bending
- Torsion
- Non-bonded: Lennard-Jones

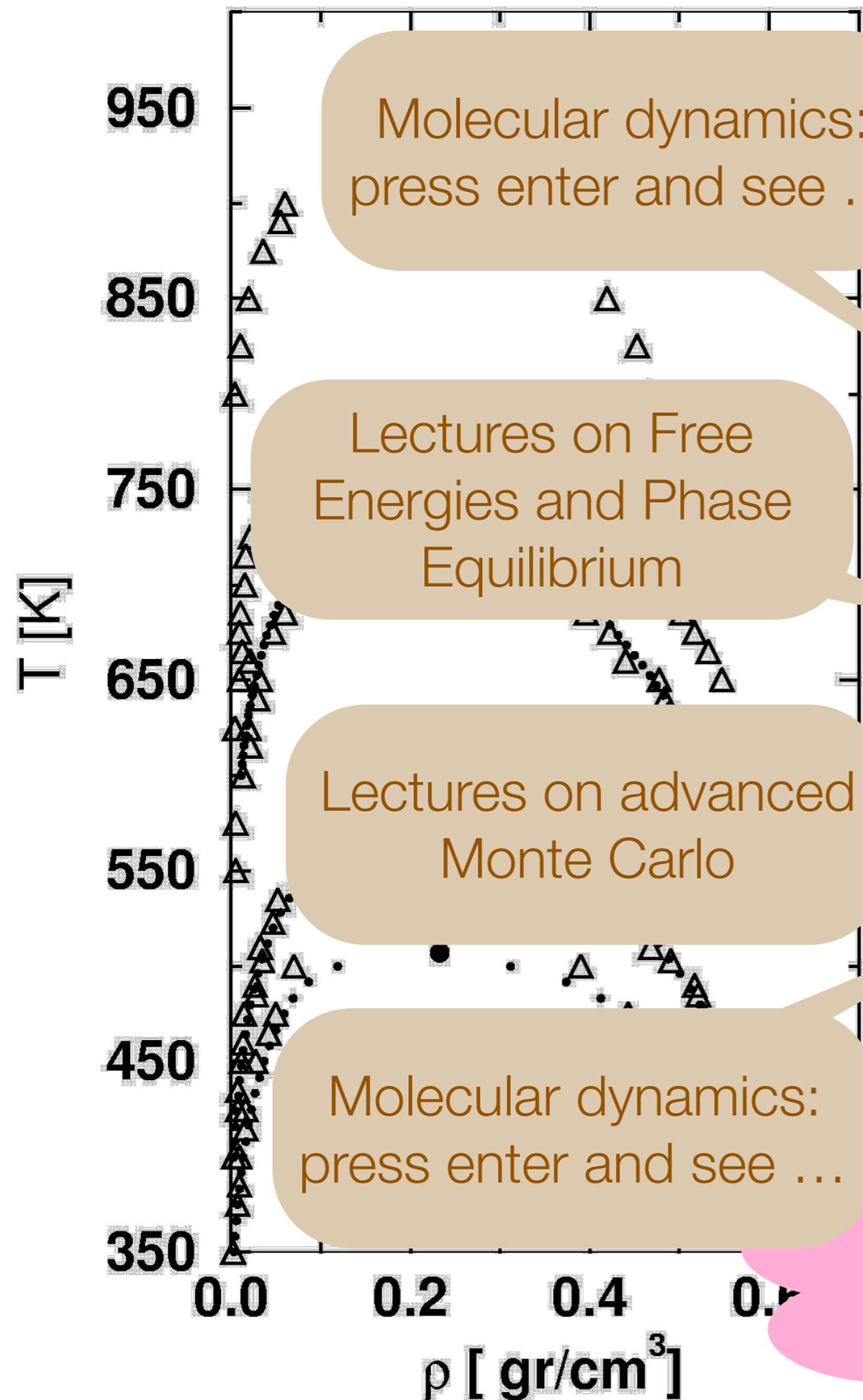


$$u(r) = 4\epsilon_{ij} \left[\left(\frac{\sigma_{ij}}{r} \right)^{12} - \left(\frac{\sigma_{ij}}{r} \right)^6 \right]$$

OPLS (Jorgensen) Model







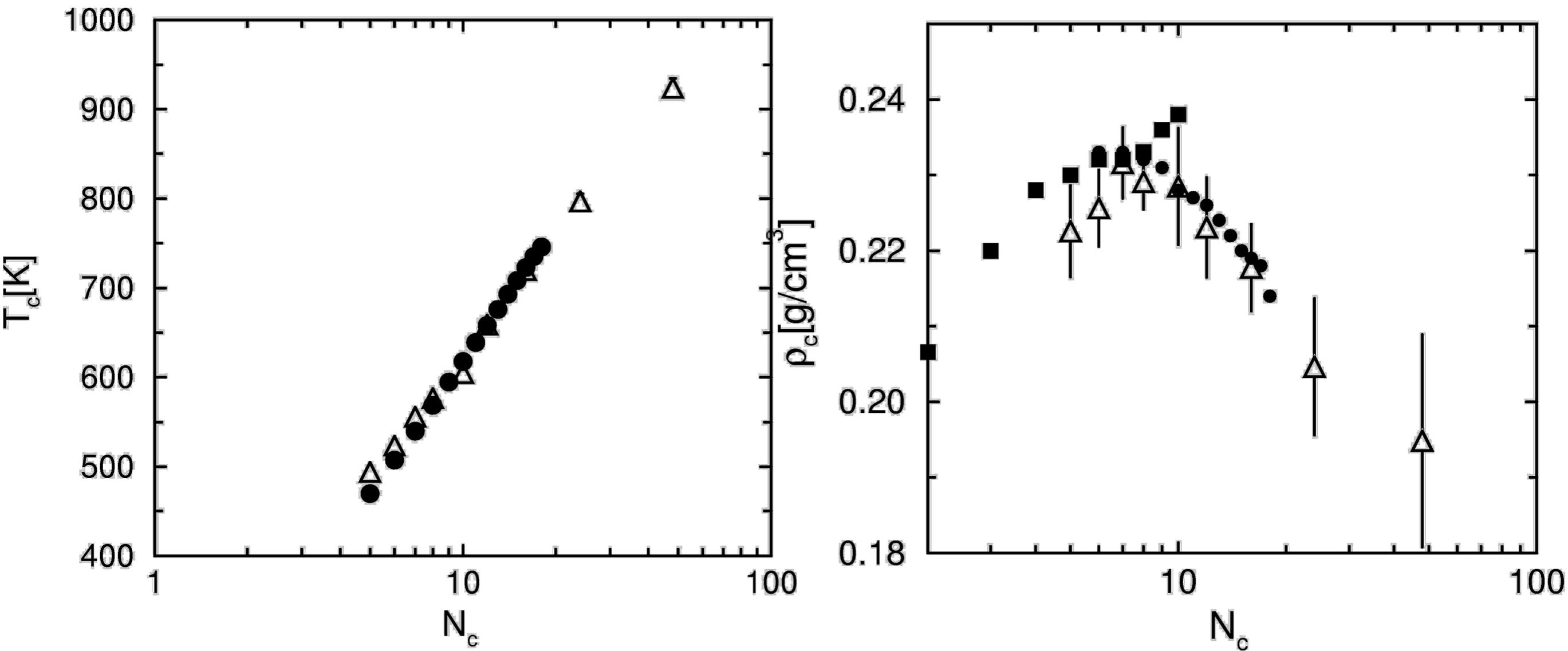
But my system is extremely small, is the statistic reliable?

Computational issues:

- How to compute vapour-liquid equilibrium?
- How to deal with long chain hydrocarbons?

But C48 moves much slower than methane (C1). Do I have enough CPU time

Critical Temperature and Density



Nature **365**, 330 (1993).

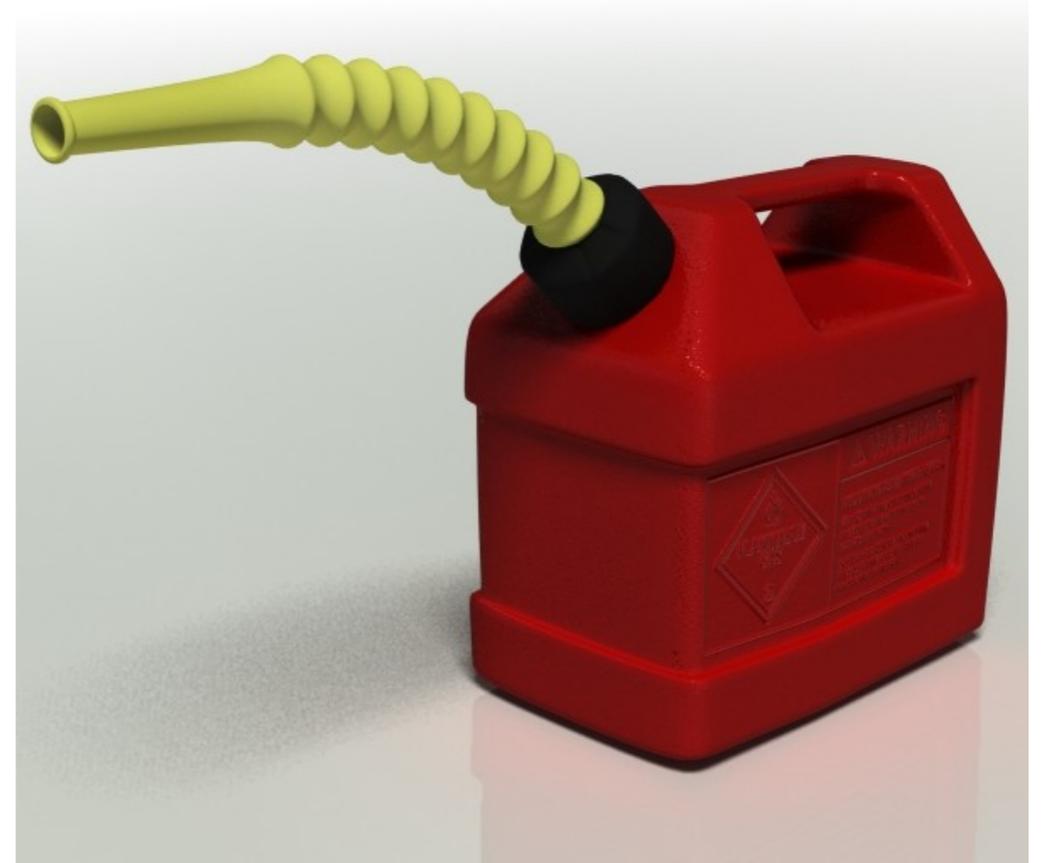
Methane storage

Methane cars: the technological obstacle

Gasoline, 1 liter

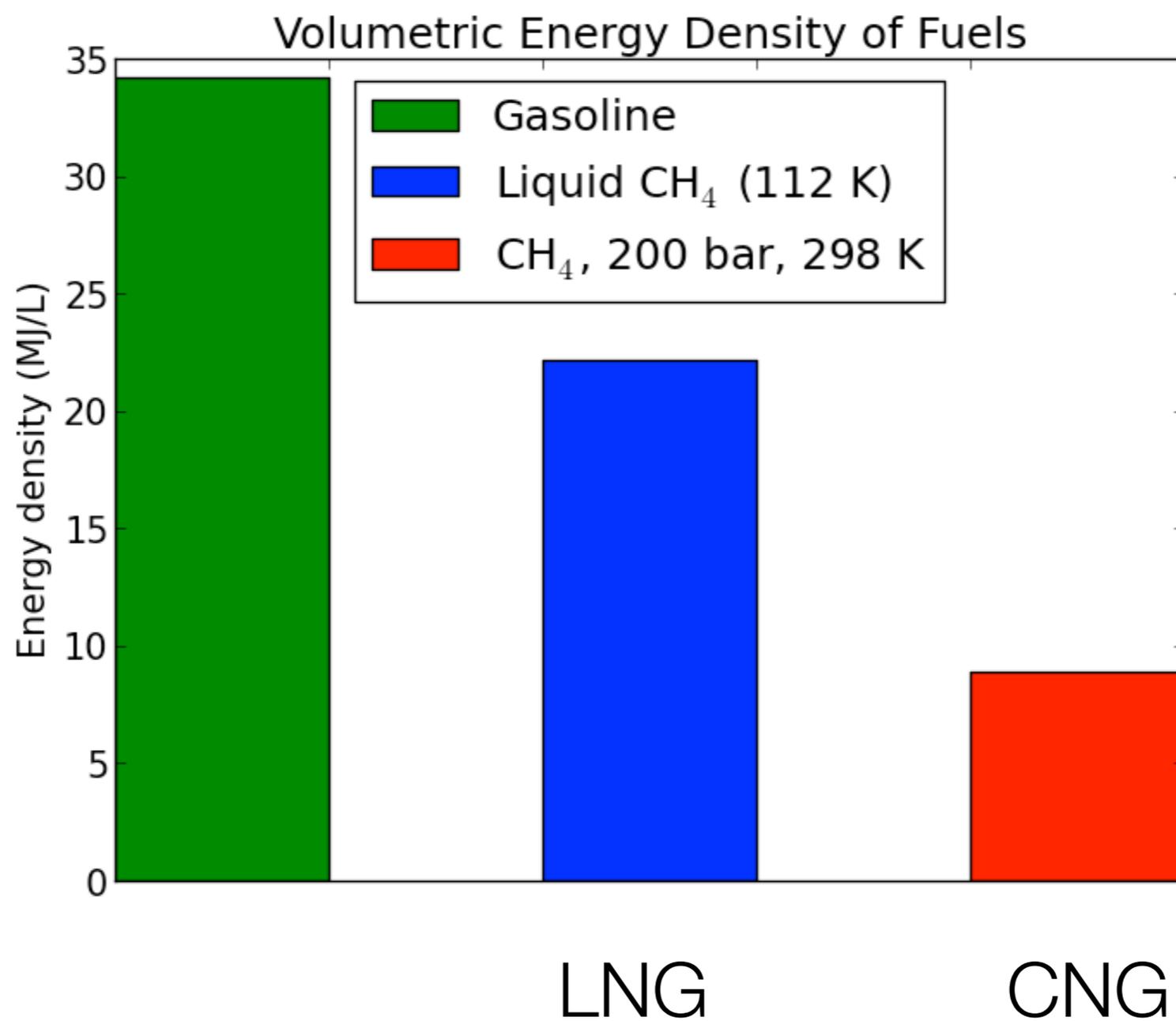


0.036 MJ



34.2 MJ

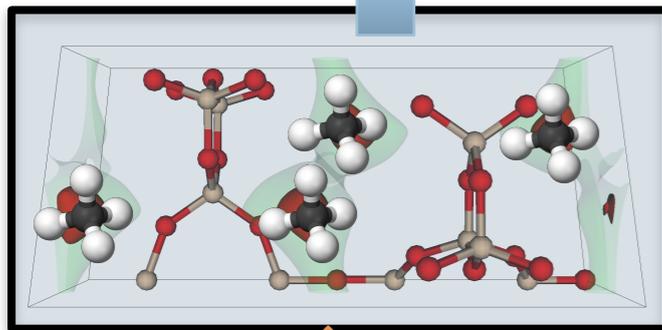
Methane versus gasoline



Pressure swing adsorption

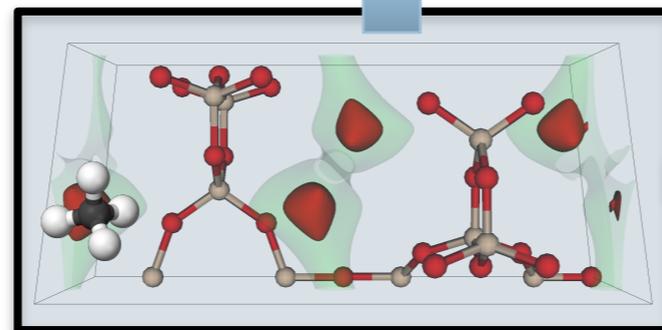


65 bar

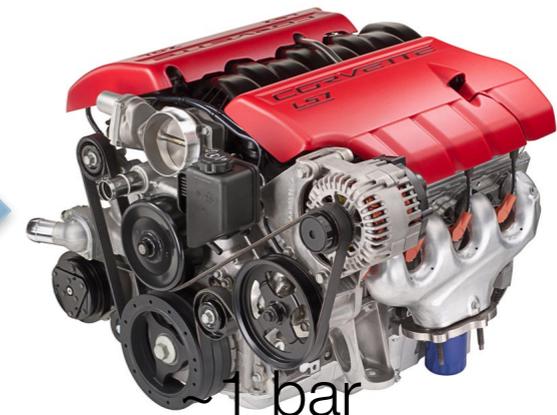
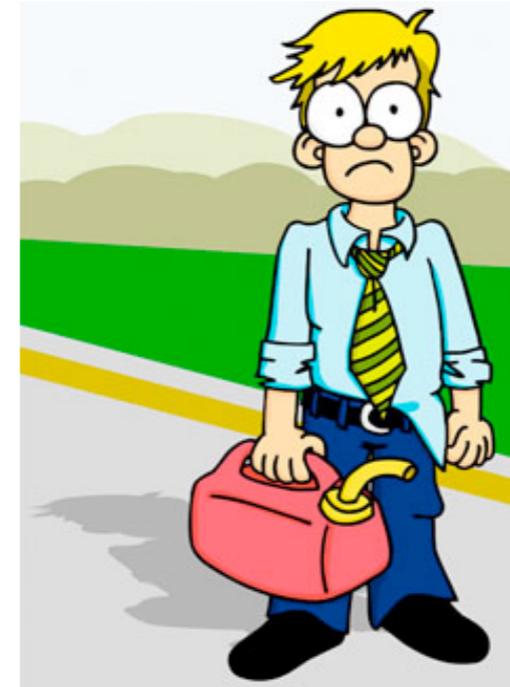


$P_H = 65 \text{ bar}$

5.8 bar



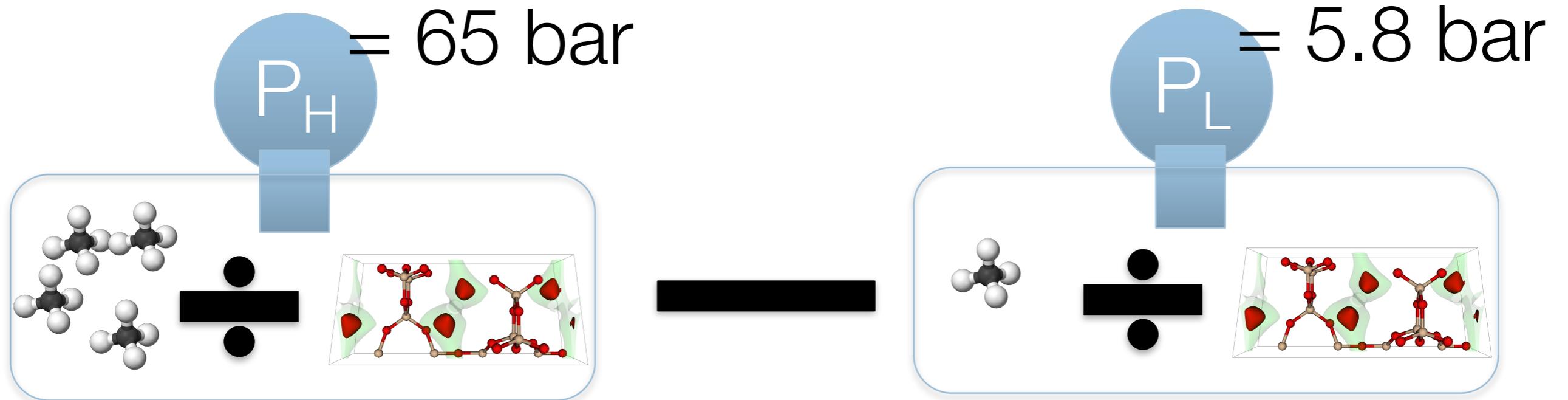
$P_L = 5.8 \text{ bar}$



Insufficient
flow

1 bar

The deliverable capacity



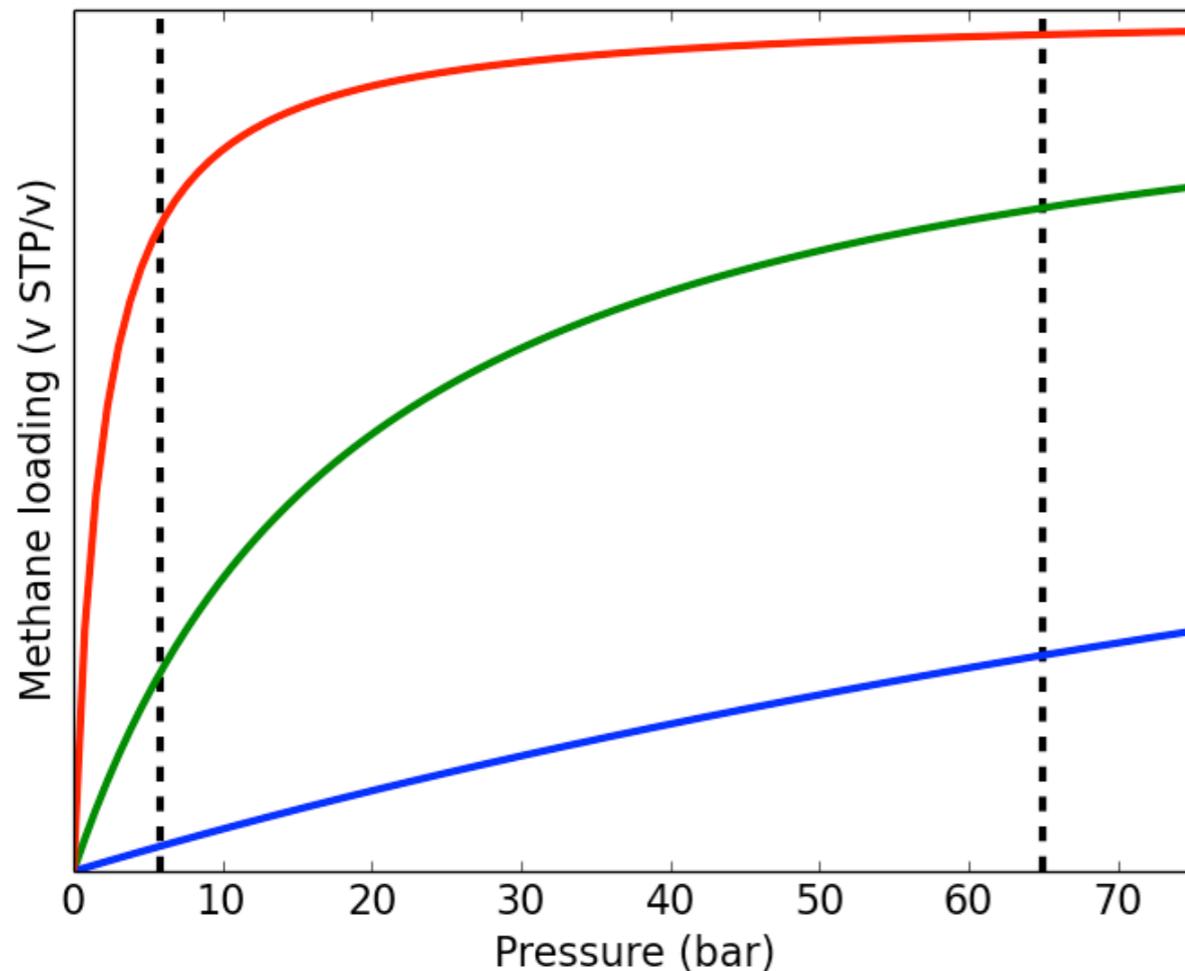
Methane adsorbed
($v \text{ STP}/v$)
at tank charging
pressure

Methane adsorbed
($v \text{ STP}/v$)
at tank discharge
pressure

ARPA-E (DOE) target: $315 \text{ m}^3 \text{ STP methane}/\text{m}^3 \text{ adsorbent}$

An optimal heat of adsorption?

Goal: maximize deliverable capacity



“For methane, an optimal enthalpy change of [16.2] kJ/mol is found.”

Langmuir 2006, 22, 1688–1700

Optimum Conditions for Adsorptive Storage

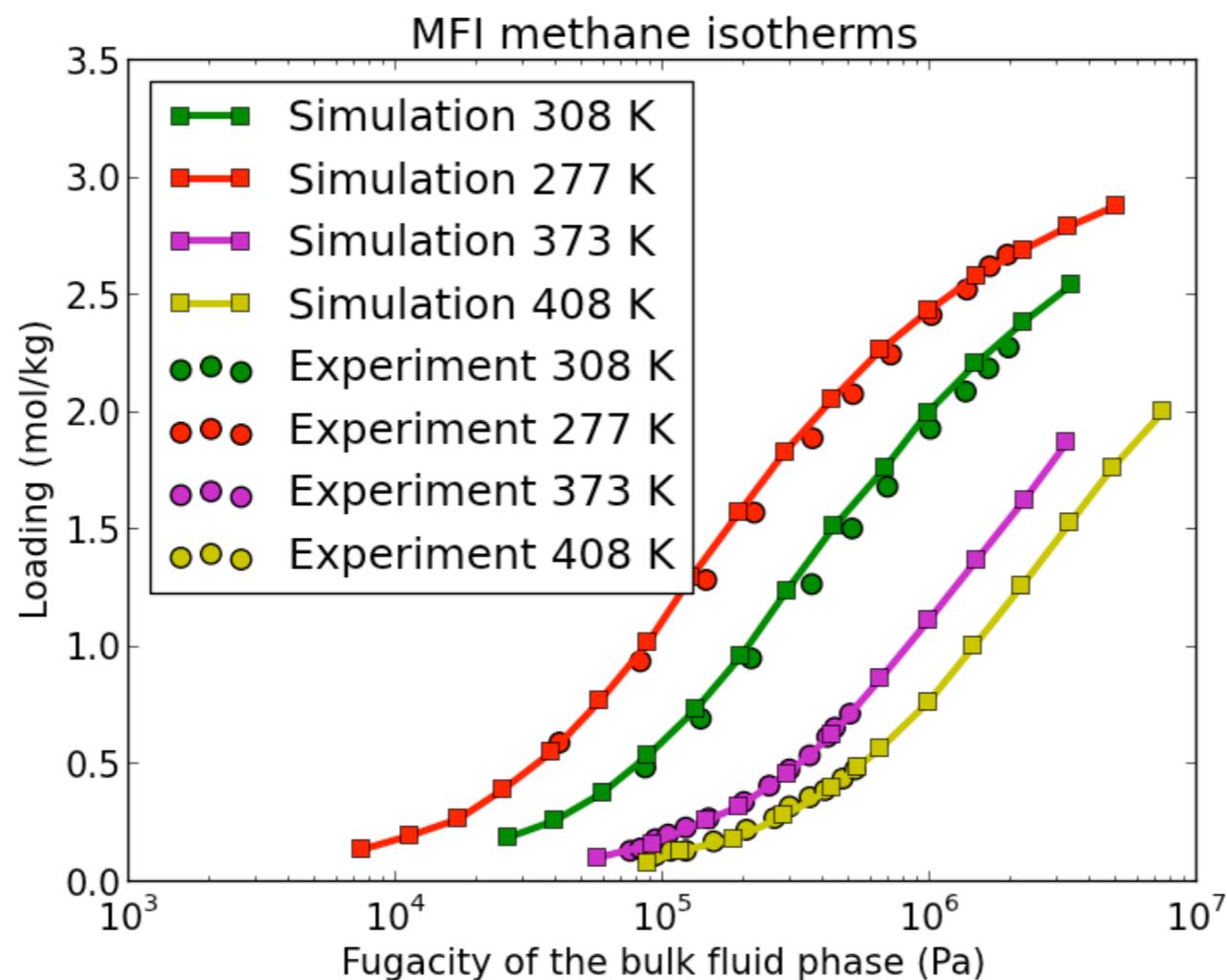
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Department of Chemical and Biomolecular Engineering, University of Pennsylvania, Philadelphia, Pennsylvania 19104

In silico screening of zeolites

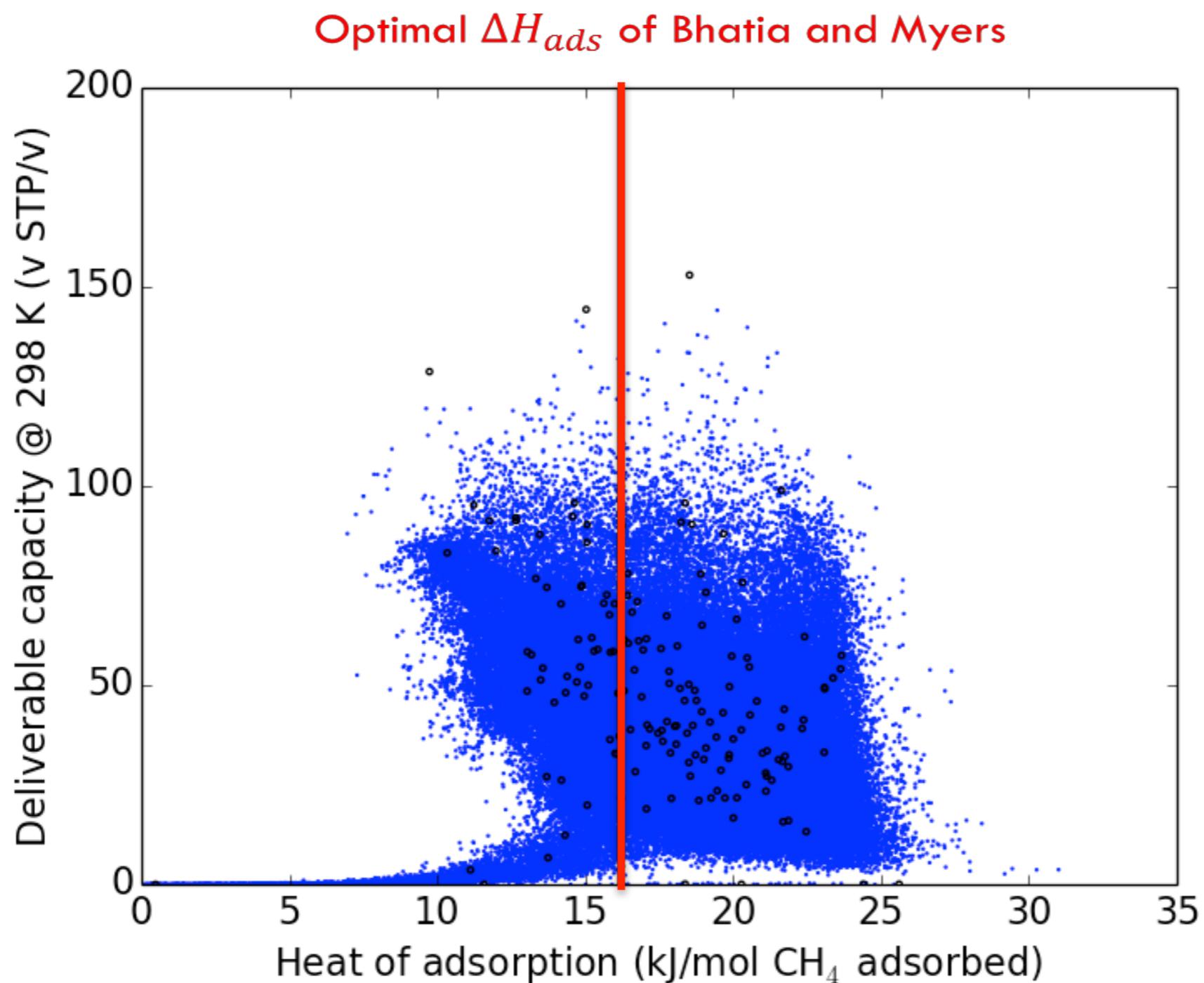


MFI expt'l data: Sun *et al.* (1998) *J. Phys. Chem. B.* 102(8), 1466-1473.

Zhu *et al.* (2000) *Phys. Chem. Chem. Phys.* 2(9), 1989-1995.

Force field: Dubbeldam *et al.* (2004) *Phys. Rev.* 93(8), 088302.

In silico screening of zeolites

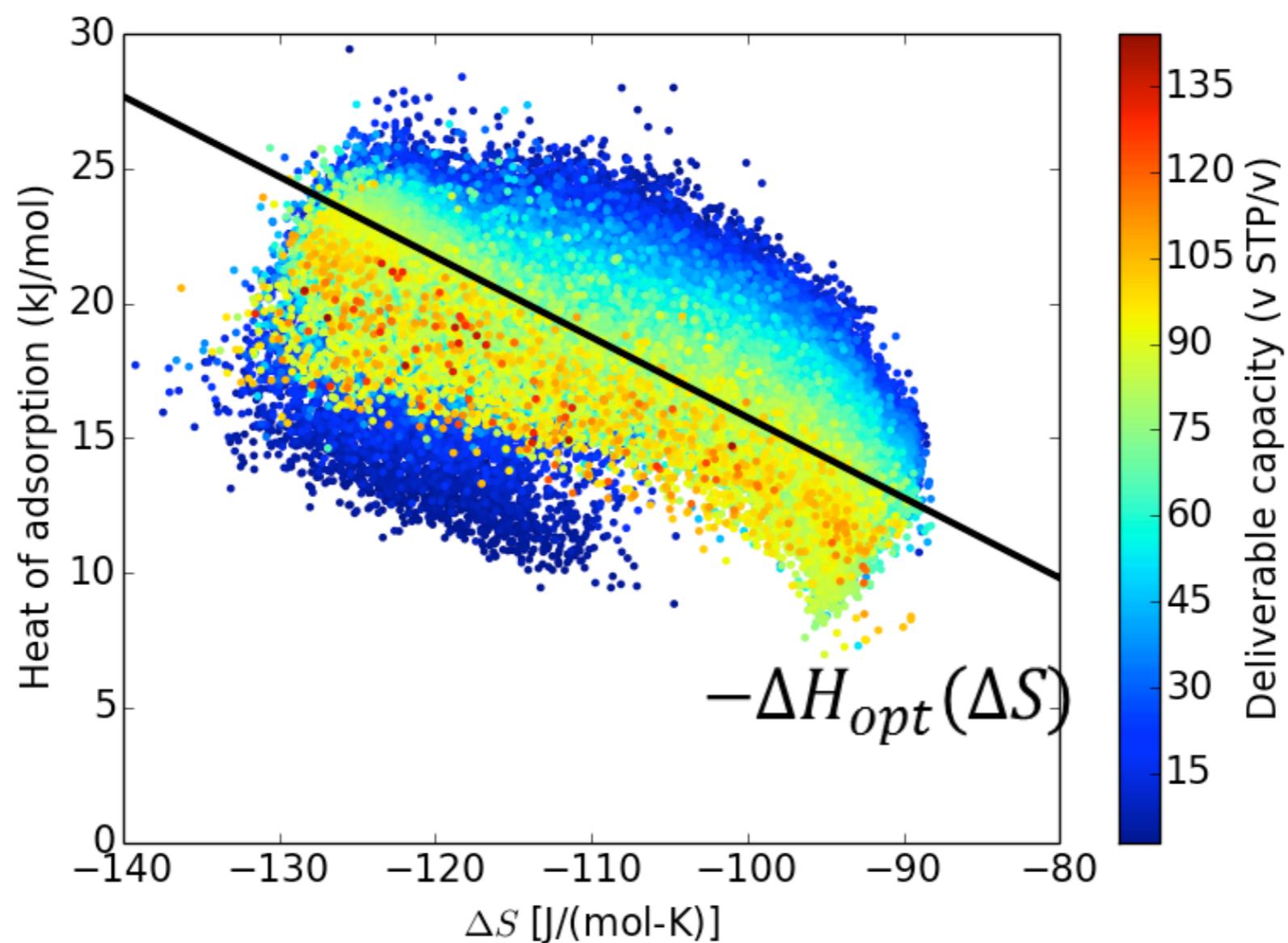


C. Simon *et al.* (2014) *Phys. Chem. Chem. Phys.* 16 (12), 5499-5513

Understanding Molecular Simulation

Enthalpy vs. entropy

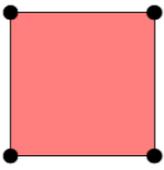
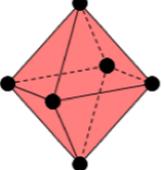
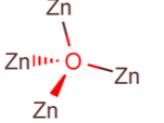
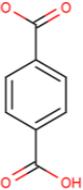
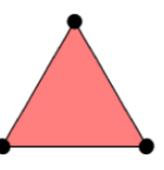
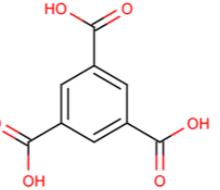
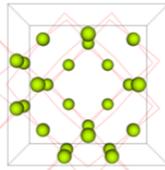
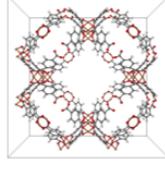
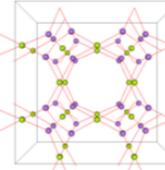
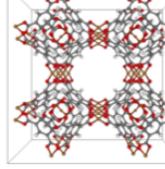
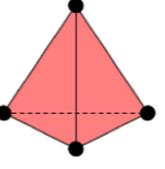
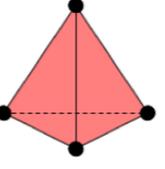
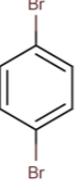
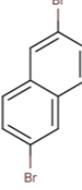
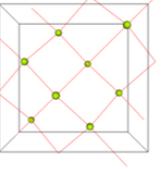
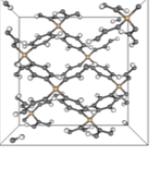
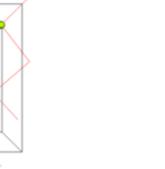
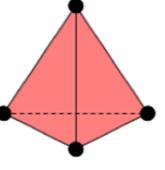
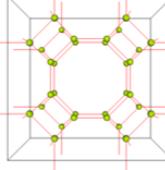
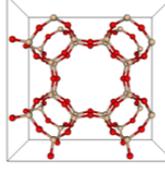
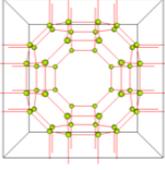
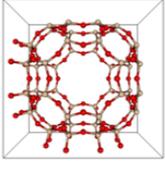
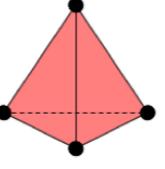
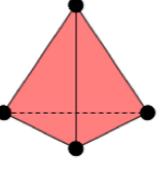
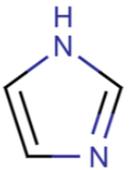
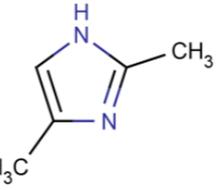
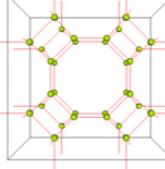
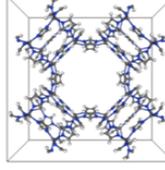
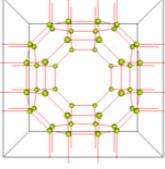
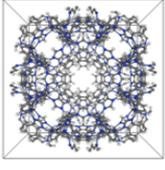
- ΔS not the same for all materials
- Wide range of ΔH that yields optimal material



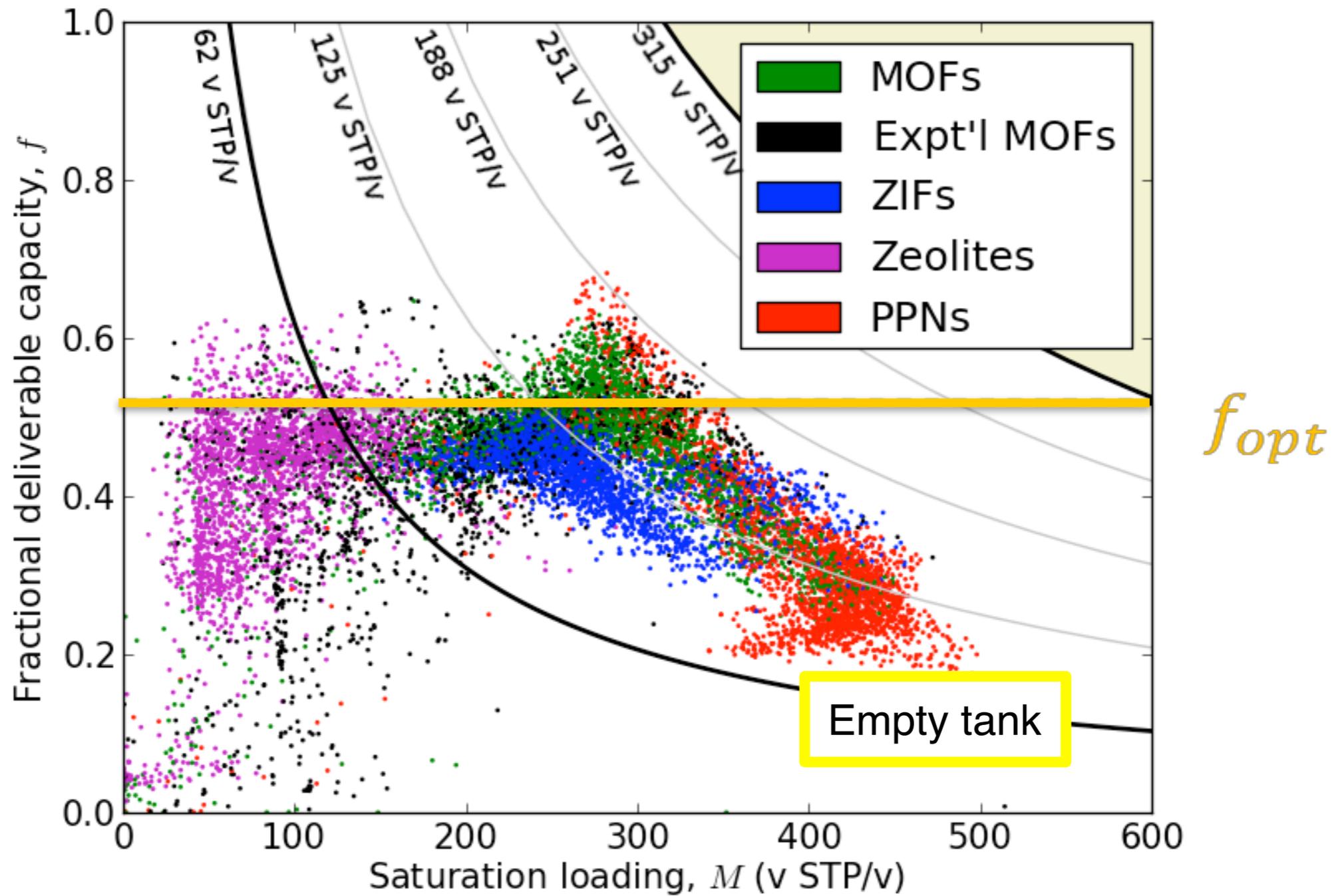
Can we find a material that meets the DOE target?

Screening > 100,000 materials

- zeolites
- Metal organic Frameworks, MOFs (Snurr and co-workers)
- zeolitic imidazolate frameworks, ZIFs, (Haranczyk)
- Polymer Porous Networks, PPNs (Haranczyk)

Material class	Building blocks				Topologies	
MOFs	 Cu—Cu	 	 	 	 	 
PPNs	 Si	 Ge	 	 	 	 
Zeolites	 Si		 O		 	 
ZIFs	 Zn	 Fe	 	 	 	 

Insight from the model



Example 3: make a model system

Question: are attractive interactions needed for a condensed phase?

YES:

- Attractive forces are needed
- Theories predict this ..

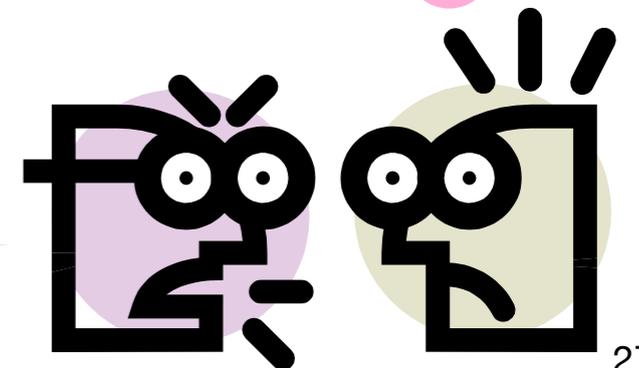
BUT:

- There are no molecules with *only* attractive interactions

How to test the theory?

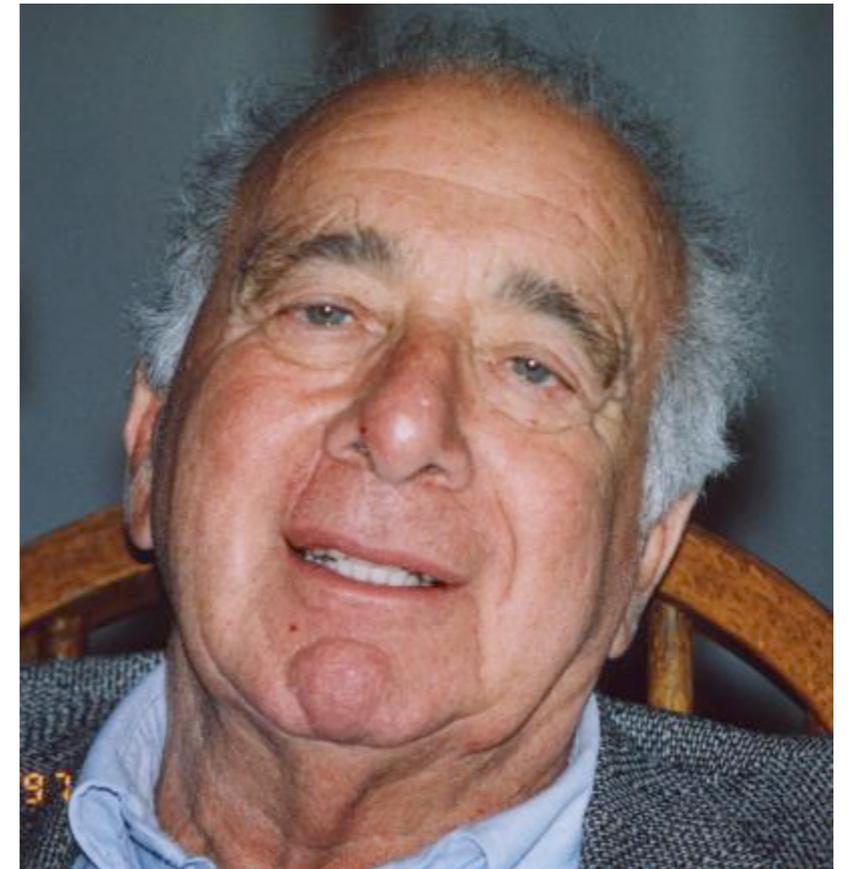
Your theory is **WRONG** it disagrees with the experiments

My theory is **RIGHT**: but this experimentalist refuses to use molecules that do not have any attractive interactions



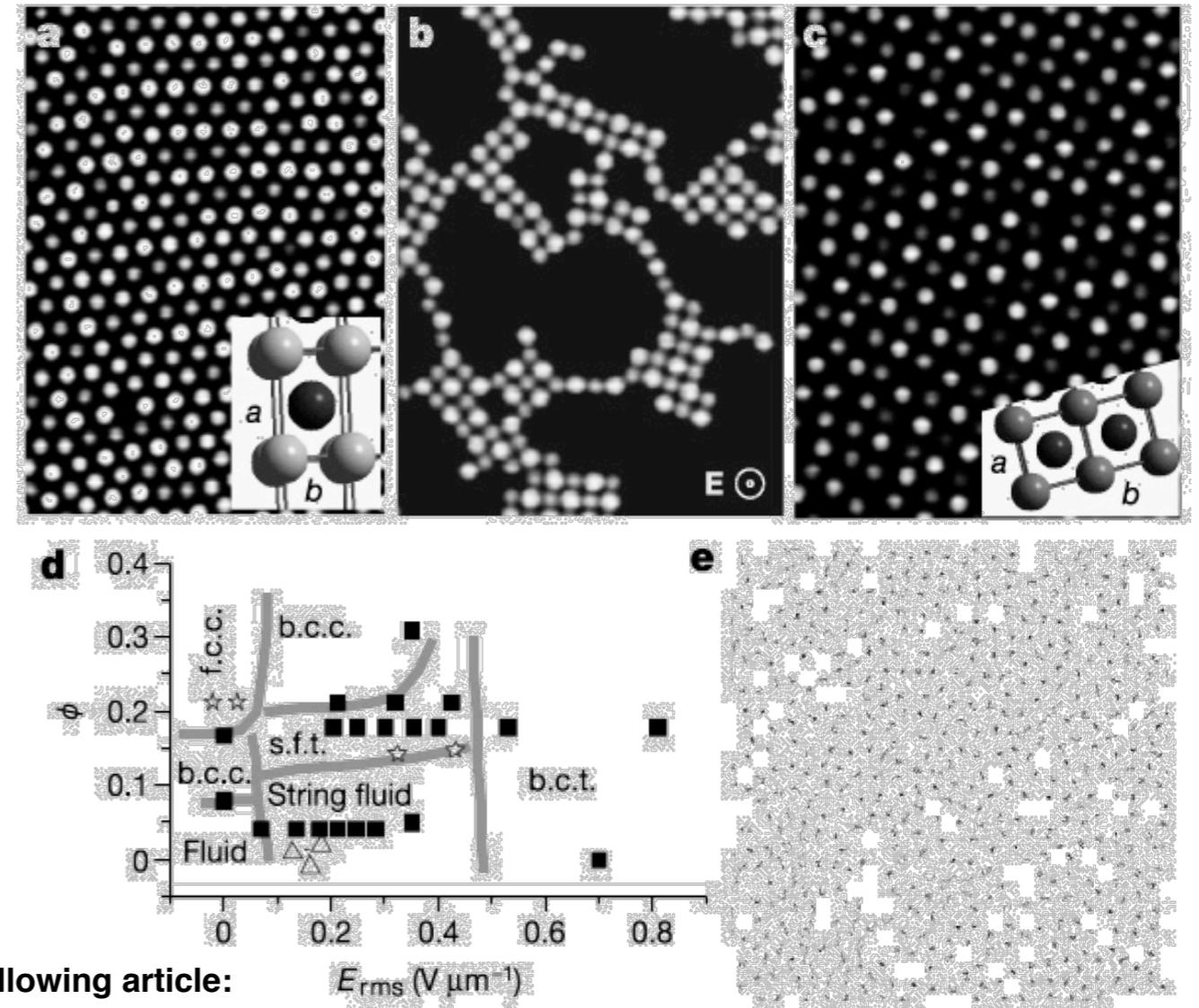
But we can simulate hard spheres ..

- Bernie Alder carried out Molecular Dynamics simulations of the freezing of hard spheres
- But, did the scientific community accept this computer results as experimental evidence ...
- ... during a Gordon conference it was proposed to vote on it ...
- ... and it was voted against the results of Alder



Experiments are now possible

.. But not on molecules
but on colloids:



From the following article:

[A colloidal model system with an interaction tunable from hard sphere to soft and dipolar](#)

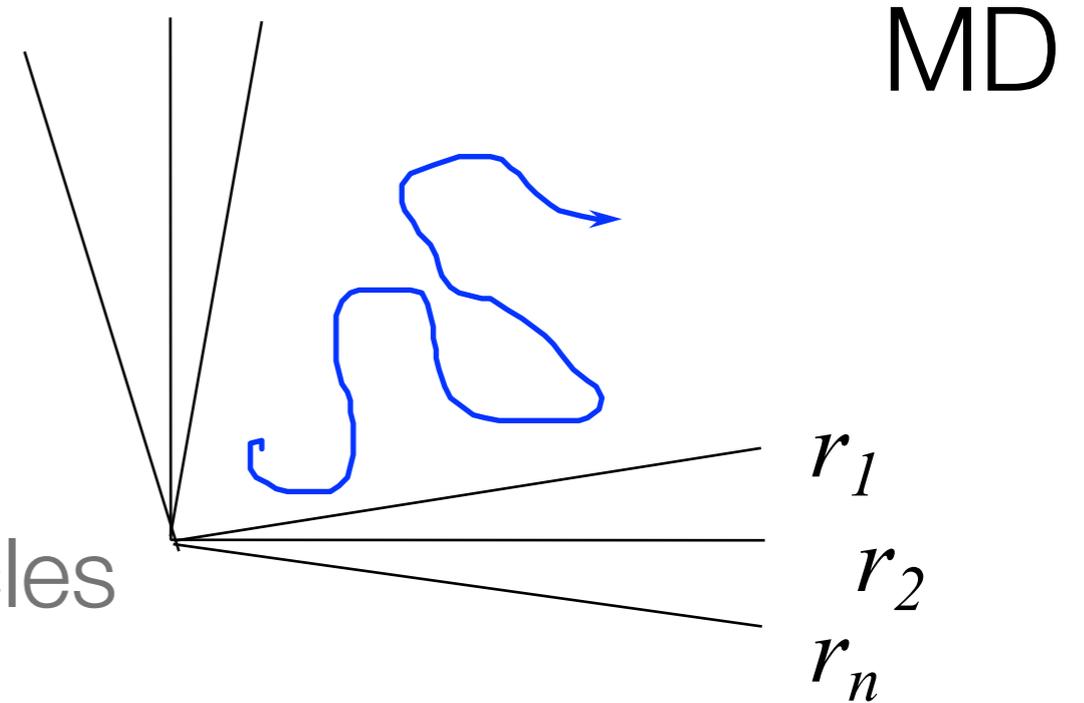
Anand Yethiraj and Alfons van Blaaderen
Nature 421, 513-517 (30 January 2003)

Molecular Dynamics

- Theory:

$$\mathbf{F} = m \frac{d^2 \mathbf{r}}{dt^2}$$

- Compute the forces on the particles
- Solve the equations of motion
- Sample after some timesteps

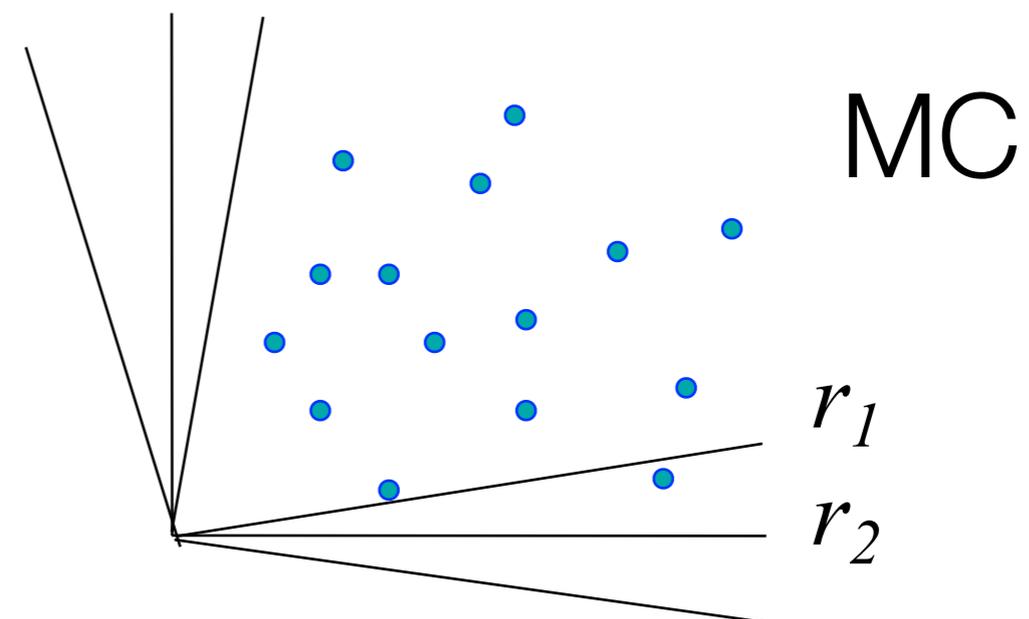


Monte Carlo

- Generate a set of configurations with the *correct* probability
- Compute the thermodynamic and transport properties as averages over all configurations

How to compute these properties from a simulation?

What is the correct probability?
Statistical Thermodynamics



Classical and Statistical Thermodynamics

Problem: we have a set of coordinates and velocities -what to do with it?

- Statistical Thermodynamics
 - The probability to find a particular configuration
 - Properties are expressed in term of averages
 - Free energies
- Thermodynamics: relation of the free energies to thermodynamic properties